



# Toward Model-Based Reconstruction in Scanned Baggage Security Applications

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## Abstract

Our research objective is a general implementation of model-based reconstruction for multi-slice helical scan CT geometry with application to transportation security screening.

Model-based reconstruction has several potential advantages compared to traditional filtered backprojection (FBP) reconstruction including:

- Reduced artifacts such as metal streaks
- Reduced noise
- Improved Image resolution

## Multi-slice helical CT

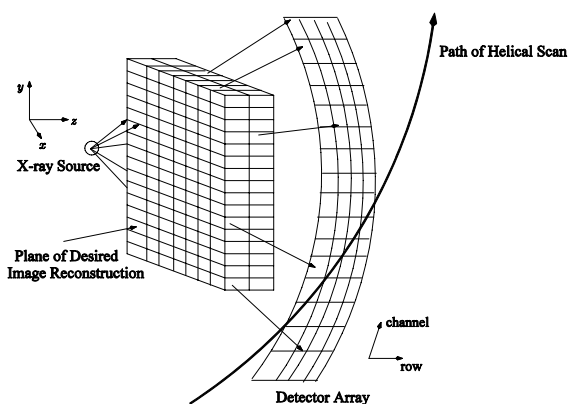


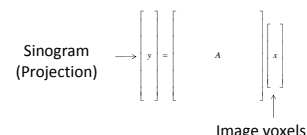
Fig 1. Multi-slice helical CT geometry

- Multi-slice helical CT has a cone-beam structure
- Gantry (X-ray source, detector array) rotates around an object in a helical scan path.
- Detector array consists of hundreds of channels and several rows.
- In our projection model, each voxel was flattened along the dimensions parallel to detector face.

## Model-based reconstruction

### Forward projection

Multi-slice helical CT scanner forward projection can be modeled by a linear matrix operation:



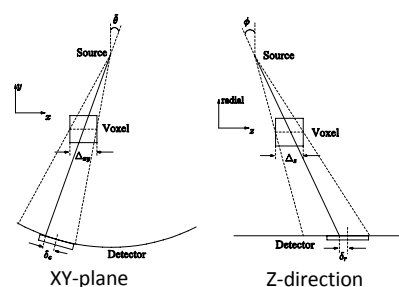
- The forward matrix A is defined by CT geometry and image representation
- The  $j$ -th column of A corresponds to projection of voxel  $j$ .
- Each column entry is calculated as a product of XY-plane projection  $B_{i,j}$ , and Z-direction adjustment factor  $C_{i,j}$  for  $i$ -th detector element.

$$A_{i,j} = B_{i,j} \times C_{i,j}$$

$$B_{i,j} = \frac{\Delta_{xy}}{\cos \theta} V_c(\delta_c) * S_c(\delta_c)$$

$$C_{i,j} = \frac{1}{\cos \phi} V_r(\delta_r) * S_r(\delta_r)$$

$\Delta_{xy}$  : Voxel size  
 $\theta, \phi$  : Ray angle in xy-plane and z-direction  
 $\delta_c, \delta_r$  : Offset from detector element center  
 $V$  : voxel window function  
 $S$  : Detector sensitivity function



### MAP estimation

$$\hat{x} = \arg \min_x \left\{ \frac{1}{2} (y - Ax)^T D (y - Ax) + U(x) \right\}$$

$x$  : Reconstructed image values  
 $y$  : Measured CT projection (sinogram)

- Log-likelihood term for x-ray transmission is based on a second-order Taylor series expansion.
- $D$  is a diagonal matrix where we assume an identity matrix.
- Log-prior  $U(x)$  is a regulation term for smoothness

### Log-prior term

We used a quadratic GMRF prior with  $p=2$  for  $U(x)$

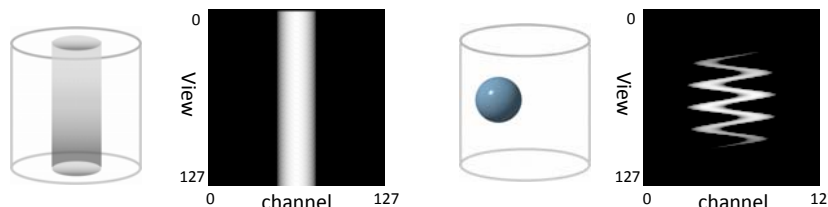
$$U(x) = \frac{1}{p\sigma^p} \sum_{(i,j) \in C} g_{i,j} |x_i - x_j|^p$$

### Optimization

Iterative Coordinate Descent (ICD) method was used  
 ICD was performed with 30 iterations

## Preliminary low resolution test results

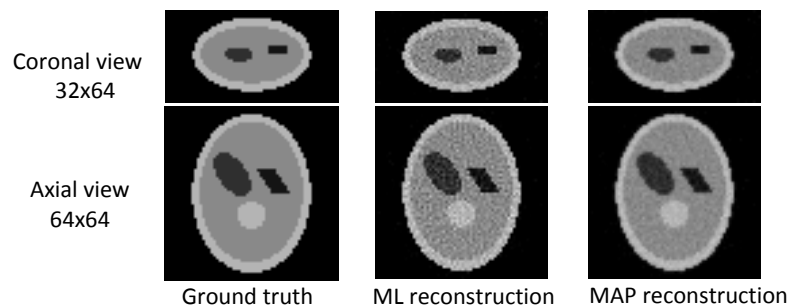
### Forward projection



(a) Cylinder object

(b) Off-centered sphere

### Model-based reconstruction (white noise was added to the simulated sinogram)



Coronal view  
32x64

Axial view  
64x64

Ground truth

ML reconstruction

MAP reconstruction

## Accomplishments

- Designed and implemented distance-driven based forward projection for multi-slice helical CT scanner
- Implemented model-based reconstruction with a quadratic prior and ICD optimization
- Simulated reconstruction using phantom data

## Future work

- Implement non-quadratic prior model
- Optimize and parallelize code
- Apply model-based reconstruction to real data
- Evaluate model-based reconstruction on a variety of real and simulated data
- Develop a statistical model for more accurate CT baggage reconstruction

## References

- J.B. Thibault, K. Sauer, C. Bouman, and J. Hsieh, "A three-dimensional statistical approach to improved image quality for multi-slice helical CT," Med. Phys., vol. 34, no. 11, pp. 4526-4544, 2007.
- K. Sauer and C. Bouman, "A local update strategy for iterative reconstruction from projections," IEEE Trans. On Signal Processing, vol. 41, no 2, 1993